

Let $X_{1:n}, X_{2:n}, \dots, X_{n:n}$ be a random sample of size n from a continuous population having pdf $f(x)$ and cdf $F(x)$. A more explicit notation of the order statistics is $X_{(1,n)}, X_{(2,n)}, \dots, X_{(n,n)}$. Where, $X_{1:n}$ = the 1st order statistic = the smallest observation = $\min(X_{1:n}, X_{2:n}, \dots, X_{n:n})$ $X_{n:n}$ = the n^{th} order statistic = the largest observation = $\max(X_{1:n}, X_{2:n}, \dots, X_{n:n})$ and $X_{r:n}$ = the r^{th} order statistic = the r^{th} smallest value

Remark 1.1. The sample observation can be arranged in ascending order of magnitude such that $X_{1:n} \leq X_{2:n} \leq \dots \leq X_{n:n}$, where the numbers $i=1, 2, \dots$, indicate the rank of the observation in the sample.

1.1 Functions of Order Statistics Range and Mid-Range: A range is the distance between the smallest observation $X_{1:n}$ and the largest observation $X_{n:n}$ observations. Thus, the sample median becomes

$$\tilde{X} = \frac{1}{2} \left(X_{\lfloor \frac{n}{2} \rfloor : n} + X_{\lfloor \frac{n}{2} \rfloor + 1 : n} \right) \quad (1.4)$$

Remark 1.2. Remark 1.3